# Coupled Multiline CW HF Lasers: Experimental Performance

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The experimental performance of two coupled arc-driven continuous wave HF chemical lasers employing unstable resonators has been measured. Mode-matched adjoint coupling of 20% was accomplished with a beamsplitter. Multiline interference fringes were obtained when the two laser output beams were overlapped in the near field. The mutual coherence of the two beams was inferred from measurement of the visibility of these fringes. Single-line fringe visibility was measured as 98% + /-2% for each of the two strongest lines. These data suggest that the two outputs are nearly completely phase locked. This locking was found to be insensitive to perturbations in the lengths of the laser resonators. Mode-beating measurements also suggest complete phase locking, since the coupled system behaves like a single laser cavity. The coherent combination of the two laser output beams was attempted by minimizing the optical path difference between these beams at an external measuring station. This was achieved by changing the external path length of one beam until maximum multiline visibility (97%) was obtained. Demonstration of the corresponding far-field peak intensity enhancement and reduction in spot size for the combined outputs was also accomplished.

#### Introduction

The larger aperture is synthesized by combining the outputs of several phase-locked smaller laser systems. Coupling of lasers is one approach to achieving the required phasing of the multiple outputs. In coupled devices, part of the output of one laser is injected into a second laser in order to achieve phase locking between the two outputs. This process is repeated for all of the lasers in the coupled system. For the purpose of this paper, we define coupling as the process of injection of part of one output into a second laser. Phase locking is defined as the achievement of complete mutual coherence between the two outputs for every spectral line. Phase matching is defined as the coherent combination (i.e., achievement of zero phase difference for all lines) of the two beams at the diagnostic location.

A theoretical investigation of coupled resonators was reported in 1972 by Spencer and Lamb. In their one-dimensional model, coupling was accomplished through a "dielectric bump" with  $\pi/2$  phase shift. This theory was extended to arbitrary phase shift by Mirels, who also investigated the effect of gain saturation on these results. All of these single-line theories predict that phase locking is sensitive to the coupling fraction and to changes in resonator length on the order of a quarter-wavelength. Palma and Fader have experimentally vertified these results using coupled single-line  $CO_2$  lasers. They found that the locking range (the distance range over which phase locking occurs) increased from a tenth-wavelength to a quarter-wavelength as the coupling fraction was increased from 9% to 50%.

The present experimental study investigates the coupling of multiline, multimode, inhomogenously broadened HF chemical lasers. The theoretical single-line results suggest<sup>2</sup> that if the resonator lengths are within the locking range for one line of a multiline laser, the other lines may or may not be within their locking ranges. This could result in about half of the output

lines being phase locked. Mirels<sup>2</sup> has suggested that mode competition may quench the unstable modes of the coupled system, in which case every output mode of the system would be phase locked, without length sensitivity or power decrement.

We have previously reported<sup>5</sup> results of preliminary experiments on two strongly coupled multiline continuous wave (CW) HF chemical lasers employing confocal unstable resonators. From measurements of the visibility of fringes obtained by overlapping the two output beams in the near field, we concluded that the multiline outputs were completely phase locked with no sensitivity to resonator length. The visibility of single-line components of the multiline interference pattern were 0.98, confirming that each line was phase locked. Measured multiline visibilities were not as high, since the path lengths for the two beams were not equalized. In this paper, we report further measurements of this strongly coupled system that verify the preceding conclusions. First, the near-field fringe scans are shown, and the maximum multiline visibility is measured by equalizing the optical path lengths for the two beams. Further evidence of complete phase locking is provided by measurements of the characteristic longitudinal mode-beat frequencies for the independent and coupled lasers. Finally, the narrowing and peak intensity enhancement of the far-field focused spot for the coupled outputs is measured. These experiments were conducted on an electric-arc-driven supersonic-diffusion CW HF chemical laser.6

## **Experimental Apparatus**

A schematic diagram of the coupled resonator configuration is shown in Fig. 1. Mirrors  $M_1$  and  $M_2$ , and  $M_3$  and  $M_4$ . comprise two nominally identical confocal unstable resonators of length 1.5 m, magnification 1.4, and equivalent Fresnel number 4.1 (based on the average wavelength of 2.8 microns and the scraper hole diameter of 7.1 mm). The resonator paths are arranged to use two separate portions of the HF gain medium. The arc-driven, supersonic diffusion HF gain generator is described in Ref. 6. The two laser outputs emerge from hole-scraper mirrors  $M_5$  and  $M_6$ , and a portion of each is directed into the other resonator through coupling beamsplitter CB. One side of CB is a 20% transmission (80% reflection) coating, and the other side is antireflection coated. The reflected component of each beam is routed to mirrors M<sub>7</sub> and M<sub>8</sub>, which become the phased array output aperture for the coupled laser system. CP is a ZnSe compensating plate in the path of one beam to provide the same dispersion encountered

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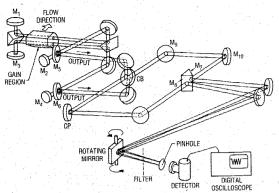


Fig. 1 Schematic diagram of the coupled unstable resonator experiment.

by the other beam, which traveled through the coupling beam-splitter before being reflected. Mirrors  $M_9$  and  $M_{10}$  are mounted together on a motorized translation stage so that the optical path length traversed by one beam can be adjusted relative to the other. The alignment of the beam as it leaves  $M_{10}$  is not affected by the path length adjustment, and so the translating combination of  $M_9$  and  $M_{10}$  is termed an "optical trombone."

The diagnostic apparatus used to characterize the two output beams included total power, beam quality, spectral line content, near-field fringe visibility, mode-beating RF spectral content, and scans of the far-field spot size. The near-field fringe scans and the far-field intensity scans were made using a rotating mirror to translate the intensity pattern over a pinhole, behind which was a Judson model LD12 indium-arsenide room temperature detector. Single-line components of the multiline pattern were obtained by inserting spectral line filters in front of the pinhole. These data were recorded on magnetic disk using a Norland 3001 digital oscilloscope. Two intracavity shutters and two external shutters facilitated comparison of the results for coupled and uncoupled operation of the individual lasers and individual and combined outputs for the coupled system.

The beam quality was evaluated by measurement of the power transmitted through an aperture whose diameter equals that of the first null in the theoretical far-field pattern. The beam quality parameter  $n^2$  is the ratio of theoretically predicted to experimentally measured power transmitted through said aperature. The theoretical values of the aperature diameter and percent power transmitted are based on a geometric optics estimate for the near-field geometry and an assumption of uniform near-field phase and intensity.

## **Experimental Results**

The individual, uncoupled beams were first characterized, displaying nearly diffraction-limited beam quality ( $n^2 = 1.02$ ). The laser line spectrum was the same whether coupled or not, with most of the power appearing on  $P_2(6)$  (comprising 36% of the output power) and  $P_2(7)$  (29%), with the remainder on  $P_2(5)$  (14%),  $P_1(5)$  (12%),  $P_2(8)$  (3%),  $P_1(7)$  (2%),  $P_2(4)$  (1.5%),  $P_1(9)$  (1%), and  $P_2(3)$  (0.5%). The laser output power was 50 W per laser when uncoupled and 75 W per laser when coupled. The power increase upon injecting 20% of one output into the other resonator indicates that the gain was not saturated by the intercavity radiation.

## Interference Fringe Visibility

Interference fringes were observed when the two output beams were overlapped in the near field. Figure 2 is a photograph of the thermal image of these fringes, and Fig. 3 shows one-dimensional centerline scans of these fringes. Figure 3a is the single-line  $P_2(6)$  component of the multiline pattern, and Fig. 3b is the multiline fringe pattern.

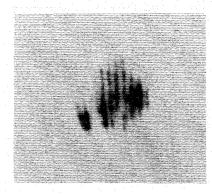


Fig. 2 Thermal image of the multiline near-field fringe pattern.

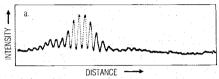


Fig. 3a Centerline scan of the  $P_2(6)$  component of the multiline near-field interference fringes.

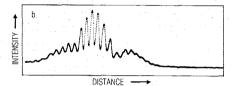


Fig. 3b Centerline scan of the multiline near-field fringes.

The visibility measured from these traces is

$$V_{\text{measured}} = (v_{\text{max}} - v_{\text{min}})/(v_{\text{max}} + v_{\text{min}})$$

where  $v_{\rm max}$  and  $v_{\rm min}$  are the maximum and minimum detector voltages measured from the zero-intensity baseline of the oscilloscope trace, respectively. The actual fringe visibility is

$$V_{\rm actual} = (I_{\rm max} - I_{\rm min})/(I_{\rm max} + I_{\rm min})$$

where  $I_{\text{max}}$  and  $I_{\text{min}}$  are the maximum and minimum intensities in the fringe pattern. The finite size of the pinhole in front of the detector results in a maximum (or minimum) voltage that is not representative of  $I_{\text{max}}$  (or  $I_{\text{min}}$ ), but is a spatial average of the intensity in the region near  $I_{\text{max}}$  (or  $I_{\text{min}}$ ). We have calculated the effect of this averaging for fringes with a cosine-wave intensity distribution and find that  $V_{\rm measured} = 0.92 V_{\rm actual}$  for the pinhole diameter (125  $\mu$ m) and fringe spacing (500  $\mu$ m) encountered in our experiments. The multiline interference fringe visibility is further degraded by a factor of 0.95 because of a small (150  $\mu$ m) difference in thickness between the coupling beamsplitter and the compensating plate. This distance mismatch results in incomplete compensation for the different phase shifts encountered by different spectral lines for the beam that goes through the coupling beamsplitter with respect to the beam that goes through the compensating plate. This calculation was made using the spectral power distribution quoted earlier and the known dispersion of the ZnSe plates. The relations between the measured and actual visibilities are thus:

$$V_{\text{single-line}} = V_{\text{measured}}/0.92$$
  
 $V_{\text{multiline}} = (V_{\text{measured}}/0.92)/0.95$ 

For Fig. 3a,  $V_{\text{single-line}}$  is 0.98, indicating nearly complete phase locking of that single-line component. An identical result was

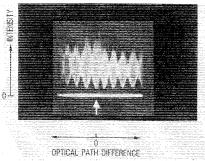


Fig. 4 Multiline fringe intensity as a function of optical path difference between the two output beams.

obtained for P<sub>2</sub>(5), suggesting that since these lines were chosen at random, all of the lines were probably phase locked. The multiline scan shown in Fig. 3b, for which  $V_{\text{multiline}} = 0.88$ , was taken without equalizing the optical path lengths for the two beams from the cavity concave mirrors to the diagnostic overlap region. The resulting phase mismatch accounts for the departure of  $V_{\text{multiline}}$  from a value near one. We verified this by stopping the rotating mirror to fix the fringe pattern in front of the pinhole and translating the optical trombone to generate the fringe minima and maxima as a function of OPD between the two beams. The measured fringe pattern vs OPD is shown in Fig. 4, for which the phase-matched central fringe is indicated by an arrow. The corrected visibility of this fringe is  $V_{\text{multiline}} = 0.97$ , indicating nearly ideal phase matching of the multiline output. This result was obtained at several values of the resonator lengths.

#### **Mode Beating**

Measurement of the difference frequencies in the laser longitudinal mode spectrum is accomplished by allowing the optical spectrum of a single spectral line [e.g., P<sub>2</sub>(6)] to beat with itself at the detector surface. The longitudinal modes resonant with a laser cavity of length L are separated in frequency by c/2L, so that if two longitudinal modes are output by the given transition, the power spectrum of the detector current will have a strong component at c/2L. A representative mode-beating measurement of the detector power spectrum is shown in Fig. 5 for one of the individual uncoupled lasers. The distance between  $M_1$  and  $M_2$  (or  $M_3$  and  $M_4$ ), is L for the individual lasers and is nominally 1.5 m. In addition to typical low-frequency beats (presumably the transverse mode spectrum), a strong component is seen near 100 MHz, precisely c/2L for a resonator 1.5 m in length. The spectrum taken for a coupled laser is shown in Fig. 6. A small component is occasionally seen at 100 MHz, but the predominant beat is at 44 MHz, implying a characteristic length of 3.4 m, which is approximately the sum of the two resonator lengths plus the coupling path length (2L plus the distance traveled through the coupling beamsplitter between M<sub>5</sub> and M<sub>6</sub>). Apparently, longitudinal modes are created that are resonant with the length of the coupled system rather than with the length of the individual resonators. This suggests that the coupled system behaves as a single-laser device with two outputs. The two outputs for such a system are completely phase locked, as they are resonant modes of a single device. Thus, the mode-beating results are independent evidence that the two outputs are completely phase locked. Again, no sensitivity to the resonator lengths was found.

## Far-Field Intensity Distribution

Finally, a far-field measurement was made to demonstrate the narrowing and peak intensity enhancement expected when two phase-matched beams are focused to a common spot. The theoretical far-field centerline scan of the focused spot for two phase-matched and two independently operating lasers is shown in Fig. 7. These calculations are based in uniform phase and intensity beams whose near-field apertures are also shown

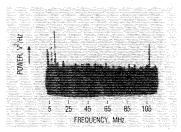


Fig. 5 Longitudinal mode-beat spectrum for an individual uncoupled laser.

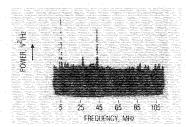


Fig. 6 Longitudinal mode-beat spectrum for an individual coupled laser.

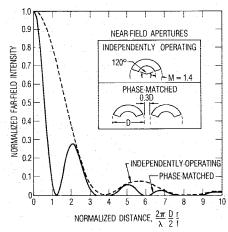


Fig. 7 Theoretical centerline horizontal scans of the far-field intensity distribution for phase-matched and for independently operating lasers.

in Fig. 7. This scan is made in the horizontal plane, as the near-field apertures are beside each other. As this figure shows, the spot corresponding to phase-matched lasers is approximately three times narrower than the spot corresponding to two independent lasers. Figure 8a shows a single-line [P<sub>2</sub>(6)] scan of the individual far-field spots of the two laser outputs, and Fig. 8b shows the single-line scan with the outputs focused to a common spot. Narrowing by a factor of 2.5 is indicated, as is the expected increase in peak intensity. This far-field measurement is extremely sensitive (on the order of a tenth-wavelength) to the external path length difference between the two beams. For a single line, this difference can be an integral number of wavelengths, while for multiline phase matching, it must be zero. The multiline result is shown in Fig. 9, for which the narrowing is a factor of 2. This result has been degraded by a global difference in OPD as well as a possible OPD mismatch on the order of a tenth-wavelength. We conclude from these far-field measurements that the expected coherent combination of the two outputs has been achieved, and that small deviations from zero OPD and wavefront aberrations account for our not achieving the theoretical maximum far-field intensity

It may also be noted from Figs. 8a and 9a that the beam quality of the individual beams is worse when coupled

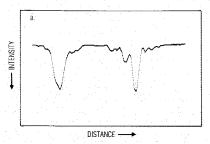


Fig. 8a Far-field scans of the  $P_2(6)$  component of the individual separated, focused spots of the two output beams.

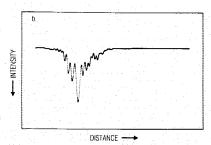


Fig. 8b Far-field scan of the  $P_2(6)$  component of the combined focused spot for the two output beams.

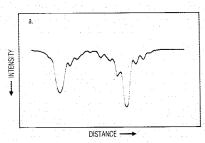


Fig. 9a Far-field scans of the multiline focused spots for the individual, separated beams.

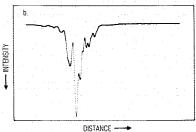


Fig. 9b Far-field scan of the multiline focused spot of the combined beams.

 $(n^2 \sim 1.8 \text{ in these figures})$  than it is uncoupled  $(n^2 = 1.02)$ . We attribute this degradation to misalignment of the coupling path between the two resonators. We have observed that the nearand far-field patterns of the coupled laser outputs are sensitive to coupling path tilt. Since the coupling beams are injected converging waves, if they are tilted with respect to the resonator optic axis, they can reinforce higher-order resonator modes that degrade beam quality.7 For our experimental geometry, we estimate a 10-urad sensitivity to tilt and millimeter position sensitivity for the alignment of the coupling paths to affect the coupled laser beam quality. This tilt tolerance is on the order of the accuracy and stability of the mirror mounts used, which may explain our difficulty in obtaining near diffraction-limited output from the individual coupled resonators. Note that phase-locking is much less sensitive to coupling path misalignment than is beam quality. This is analgous to the beam quality degradation that occurs in a ring resonator when the reverse wave suppressor mirror is tilted. Thus, the alignment sensitivity of the coupling path is roughly twice that of the individual resonators.

#### **Conclusions**

The measurements reported in this paper pertain to the use of coupled lasers in a phased array. Such an array requires both phase locking and phase matching of the multiple outputs. Our measurements confirm that both conditions can be achieved. We have shown, with the measurements of single-line near-field fringe visibilities and mode beating, that phase locking occurs in our strongly coupled system without resonator length sensitivity. Our multiline fringe visibility measurements and the far-field scans demonstrate that phase matching of the two outputs requires submicron length control of their external paths. Thus, phased laser array performance is most sensitive to external path length equalization, with tilt sensitivity next, while their sensitivity to wavefront aberrations is an order of magnitude less. 9

The coupling fraction of 20% used in the present study represents strong coupling, since the injected component from one laser makes several passes through the gain region of the second laser before collapsing onto the optic axis of the second resonator, where the output mode of the resonator is established. The original 20% of the laser intensity is amplified by an order of magnitude or more on its way in and out of the second resonator. Such high intensity, injected onto the optic axis of each resonator by the other, is probably the reason that complete phase locking occurs, and the coupled system behaves as a single-laser device. We expect that as the coupling fraction is decreased, length sensitivity will increase, and ultimately independent operation of the two devices will occur.

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